## **Topics in Algebra**

2 units (selection)

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**Target**) To learn some combinatorial techniques based on the theory of partitions.

**Outline**) A partition of a natural number n is any non-increasing sequence of natural numbers whose sum is n. For example, there are three partions of 3, because 3=2+1=1+1+1. This class introduces some combinatorial techniques and tools such as generating functions based on several topics from the theory of partitions.

**Style**> Lecture

Keyword integer partition, generating function

Fundamental Lecture "Basic Mathematics/Calculus 1"(1.0)

**Goal**) To learn some combinatorial techniques and tools such as generating functions.

## Schedule>

- 1. Some terms from set theory
- 2. Euler's identity
- **3.** Ferrars graph
- 4. Generating function
- **5.** Euler's theorem
- 6. Two variable generating function
- 7. Euler's pentagonal number theorem
- 8. Congruences
- 9. The Rogers-Ramanujan identities I
- 10. Formulas of partition functions
- **11.** q-binomial coefficients
- 12. q-binomial theorem
- 13. Jacobi's triple product identity
- 14. The Rogers-Ramanujan identities II
- 15. Applications
- **16.** Summary

**Evaluation Criteria** Assignments count 100%.

**Textbook**⟩ Integer partitions. George Andrews, Kimmo Eriksson, Cambridge University Press

**Reference**> An introduction to the theory of numbers. G. H. Hardy, E. M. Wright, Oxford University Press

**Contents**> http://cms.db.tokushima-u.ac.jp/cgi-bin/toURL?EID=216751 **Contact**>

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