Topics in algebra and analysis

2 units (selection)

YOShinori Mizuno - Associate Professor / Electrical and Electronic Systems, Electrical and Electronic Engineering, Systems Innovation Engineering

Target) We will learn some important properties of a special function, which is called the Riemann zeta function. Further we will learn how to solve problems produced by this function.

Outline) We will learn developement of mathematical tools in order to prove some properties of the Riemann zeta function, such as the special values, Euler product and the functional equation.

Fundamental Lecture) "Basic Mathematics/Calculus 1"(1.0), "Basic Mathematics/Calculus 2"(1.0), "Complex Analysis"(1.0)

Relational Lecture "Numerical Analysis" (0.5)

Goal) We will learn fundamentals of modern abstract mathematics and realize its effectiveness.

Schedule>

- 1. Introduction
- 2. Zeta function
- **3.** Leonhard Euler
- 4. Special values
- 5. Analytic continuation
- 6. Special values and analytic continuation
- 7. Euclid's proof
- **8.** Fermat prime
- 9. Euler product
- 10. Prime number theorem I
- 11. Prime number theorem II
- 12. Prime number theorem III
- **13.** Functional equation I
- **14.** Functional equation II
- **15.** Summation
- **16.** Assignments

Evaluation Criteria) Evaluation will be based on assignments.

Reference> Dunham, William, "Euler: the Master of Us All", The Mathematical Association of America

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